

Investigation of the use of deflections of vertical measured by DIADEM camera in the GSVS11 Survey

**YM Wang¹ , X Li² , S Holmes³ , DR Roman¹ , DA Smith¹ , S
Guillaume⁴ and B Bürki⁴**

¹ National Geodetic Survey, NOAA, USA

² ERT Inc. USA

³ SGT Inc. USA

⁴ Institute of Geodesy and Photogrammetry, Federal Institute of Technology
Zürich, Switzerland

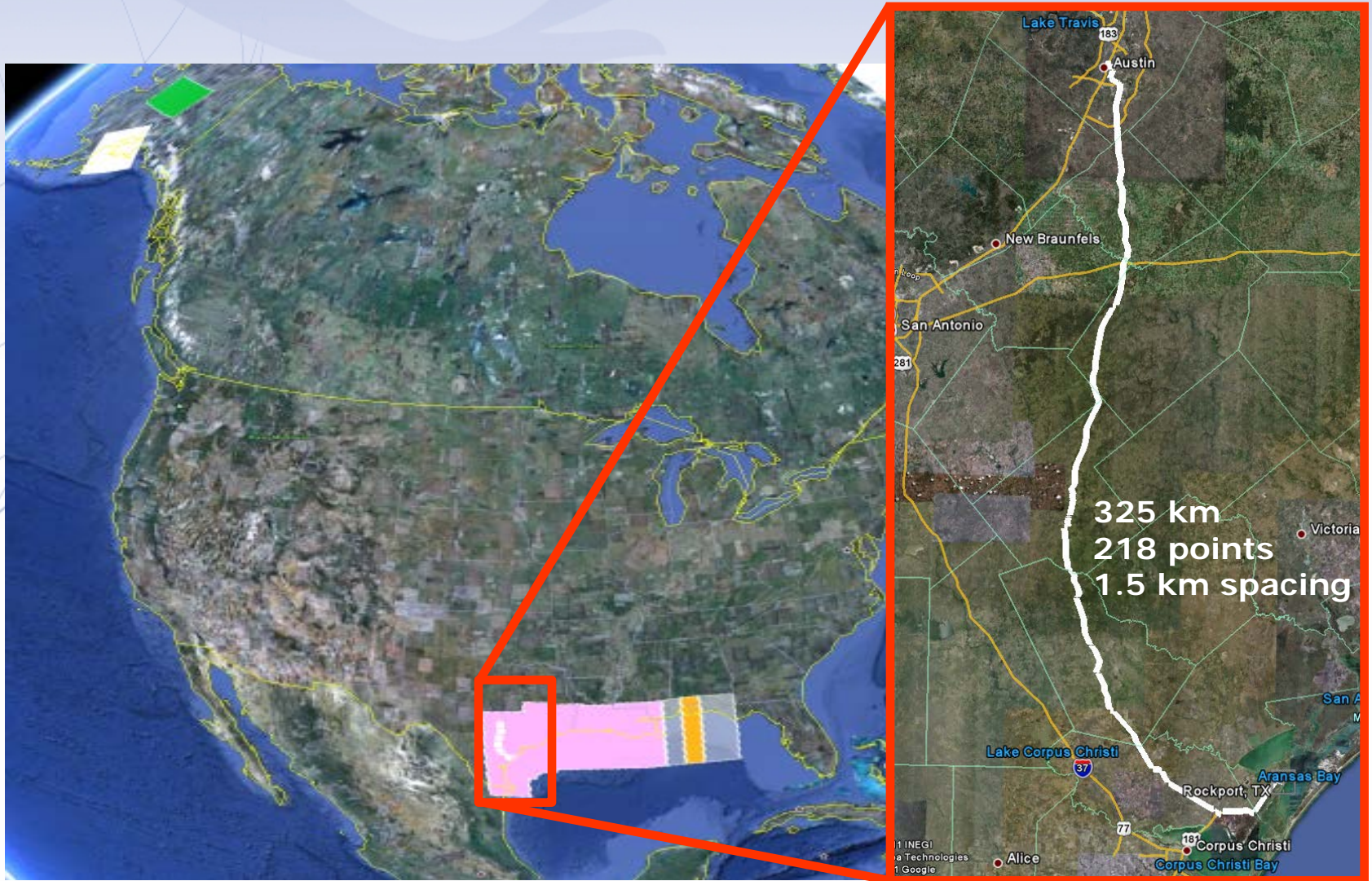
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Outline

- Goal: to compute a geoid profile of 325 km long to the sub-cm differential accuracy using GSVS11 data (GPS, Leveling, DoV, gravity, DEM data)
- Data accuracy of GSVS11
- Geoid computation using DoV data, and the effect of the systematic bias on the geoid along the line
- Geoid profile using spectral combination of GPSL and DoV
- Geoid models evaluation and differential accuracy estimation
- Conclusions and future work

Location of GSVS11



Accuracy of gravimetric and geometric data of GSVS11

At each benchmark (~1 mile spacing along the line):

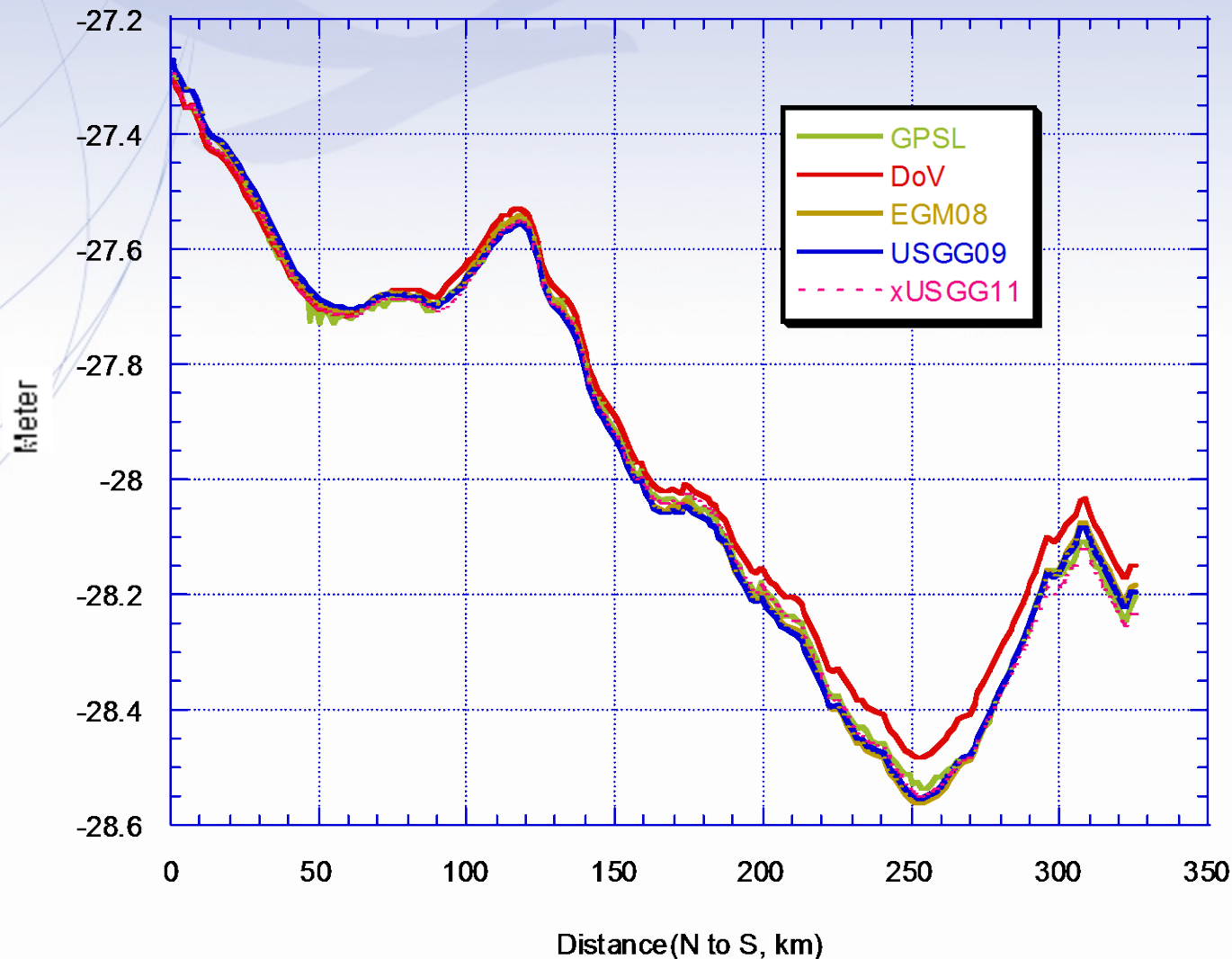
- Ellipsoidal height (24-48 hours GPS obs. time), OPUS project used for data processing ($\sigma = \pm 3-4$ mm)
- Leveled elevation of the 1st order class II specification ($\sigma = \pm 0.7\sqrt{d}$ mm, ~13 mm over 325 km)
- DoV observations by DIADEM camera ($\sigma = \pm 0.1''$)
- Absolute and relative gravity ($\sigma < \pm 20$ microGal)

DoV geoid profile computation

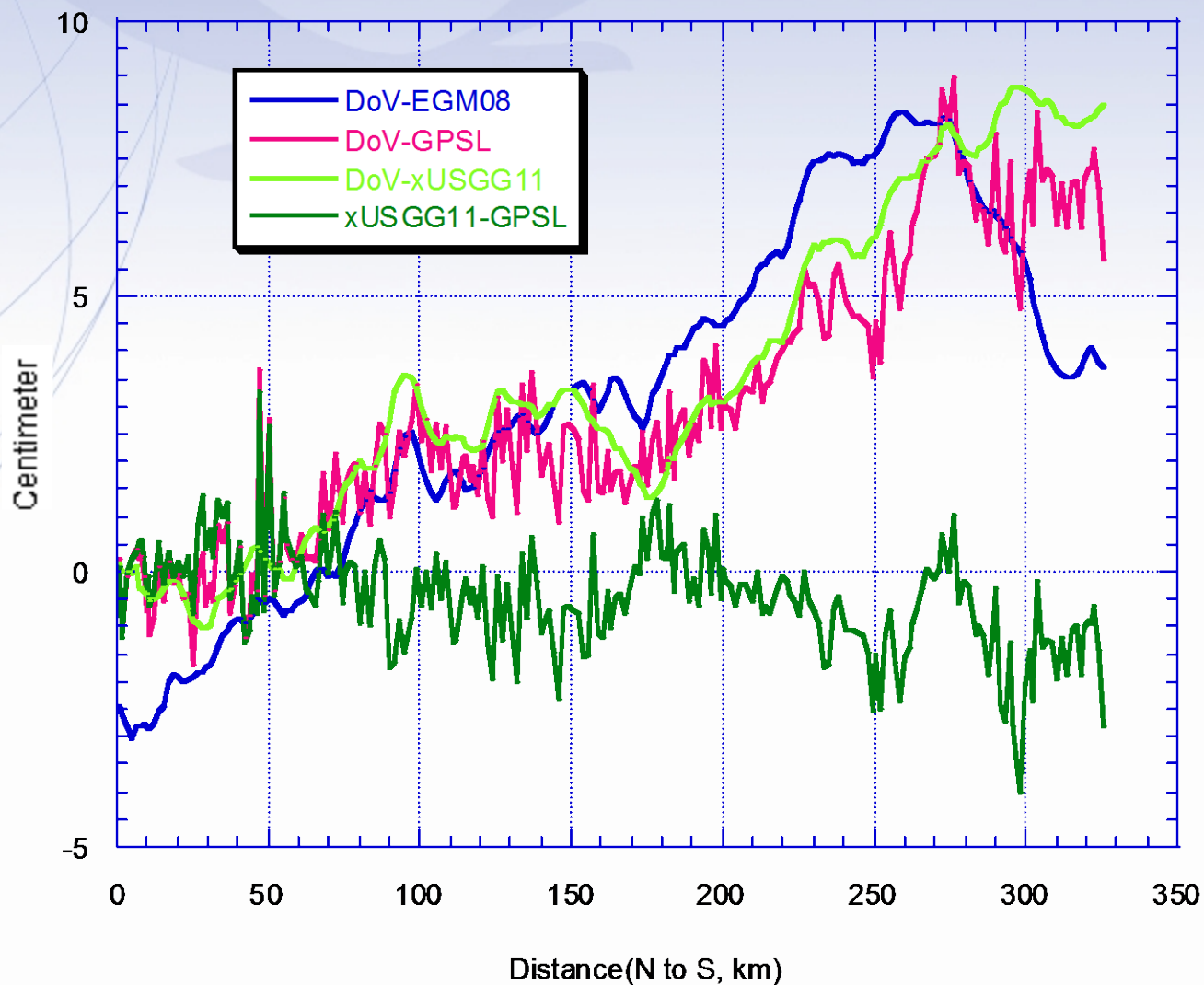
Dynamic method (Hoffmann-Wellenhof and Moritz, 2006, chapter 8.13)

1. Correct the normal gravity curvature from the observed surface DoV
2. Compute the height anomaly using the corrected DoV, take into account the height changes of the topography (non-equipotential surface)
3. Convert the height anomaly into the geoid using the Bouguer anomaly

Geoid Profiles



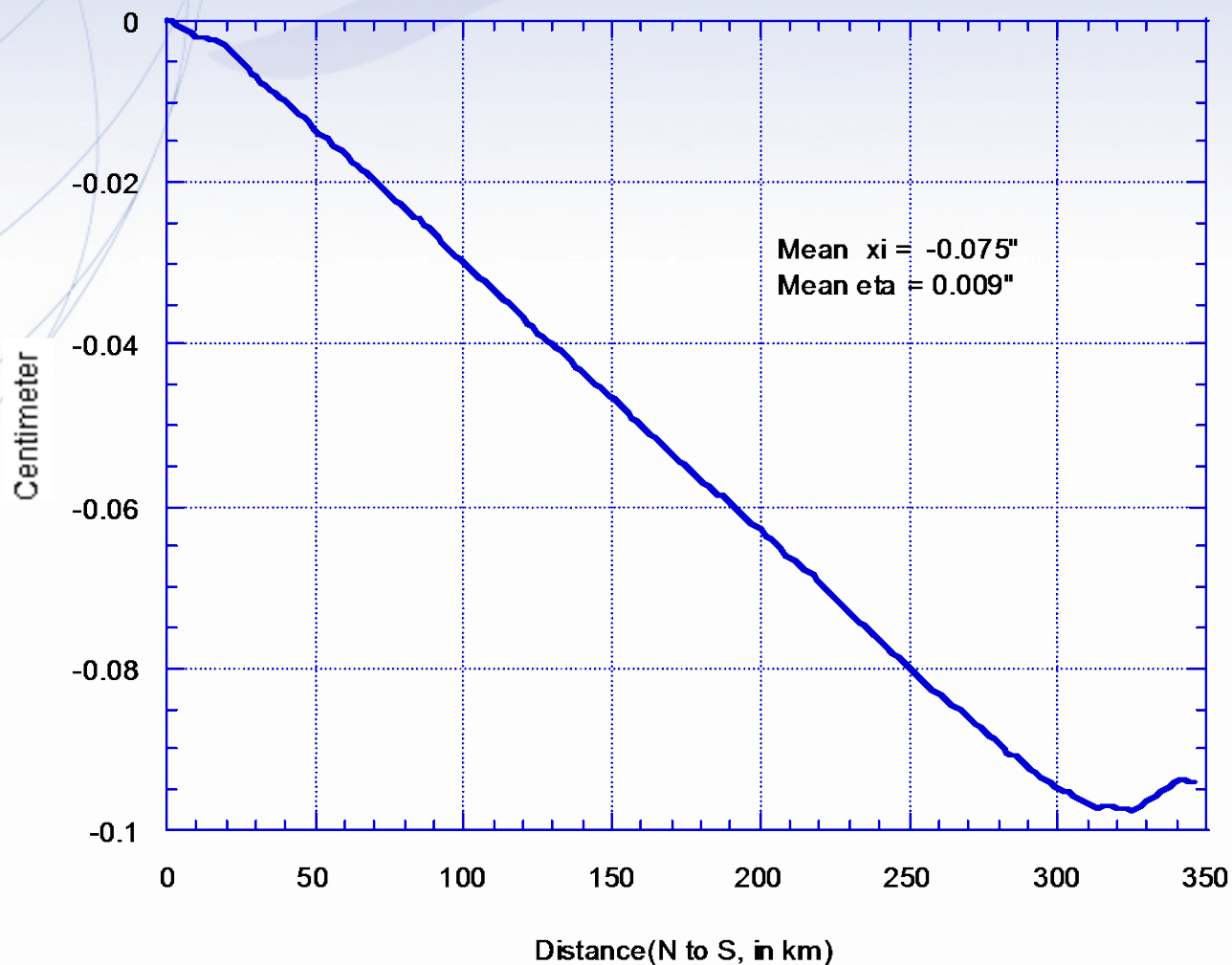
Geoid differences



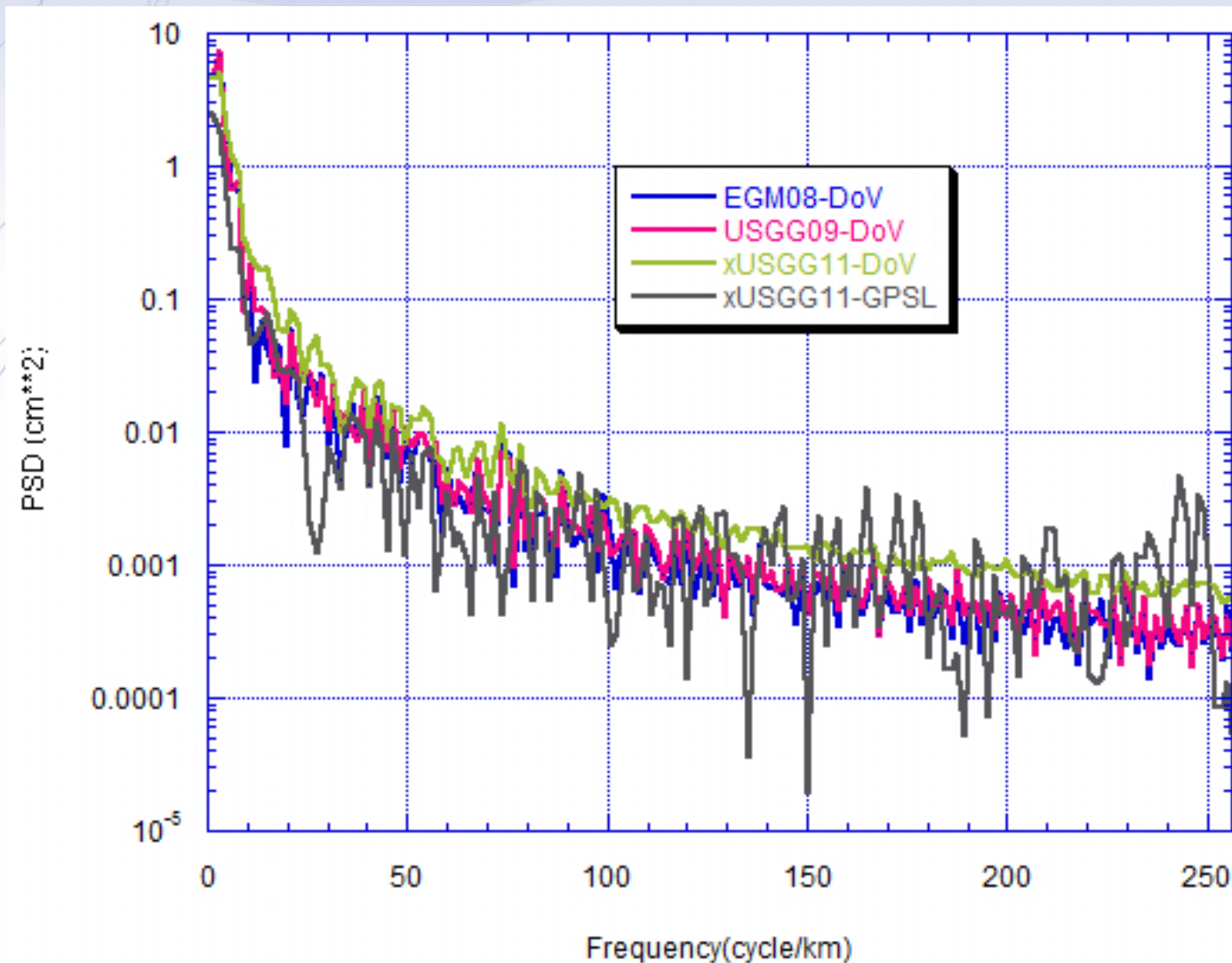
Geoid differences (in mm)

	GPSL- DoV	USGG09- DoV	EGM08- DoV	xUSGG11 -DoV	xUSGG11 -GPSL
Mean	-29.7	-30.2	-29.6	-34.5	-4.8
STD	25.4	33.0	32.6	29.6	9.5
RMS	39.1	45.0	44.1	45.5	10.7
Min.	-16.7	-77.0	-83.0	-88.0	-40.4
Max.	89.3	28.0	30.0	10.0	32.8

Contribution of “suspected” biases in DoV data to the geoid



Power spectral density (PSD) of the residual geoids



Spectral combination (GPSL+DoV)

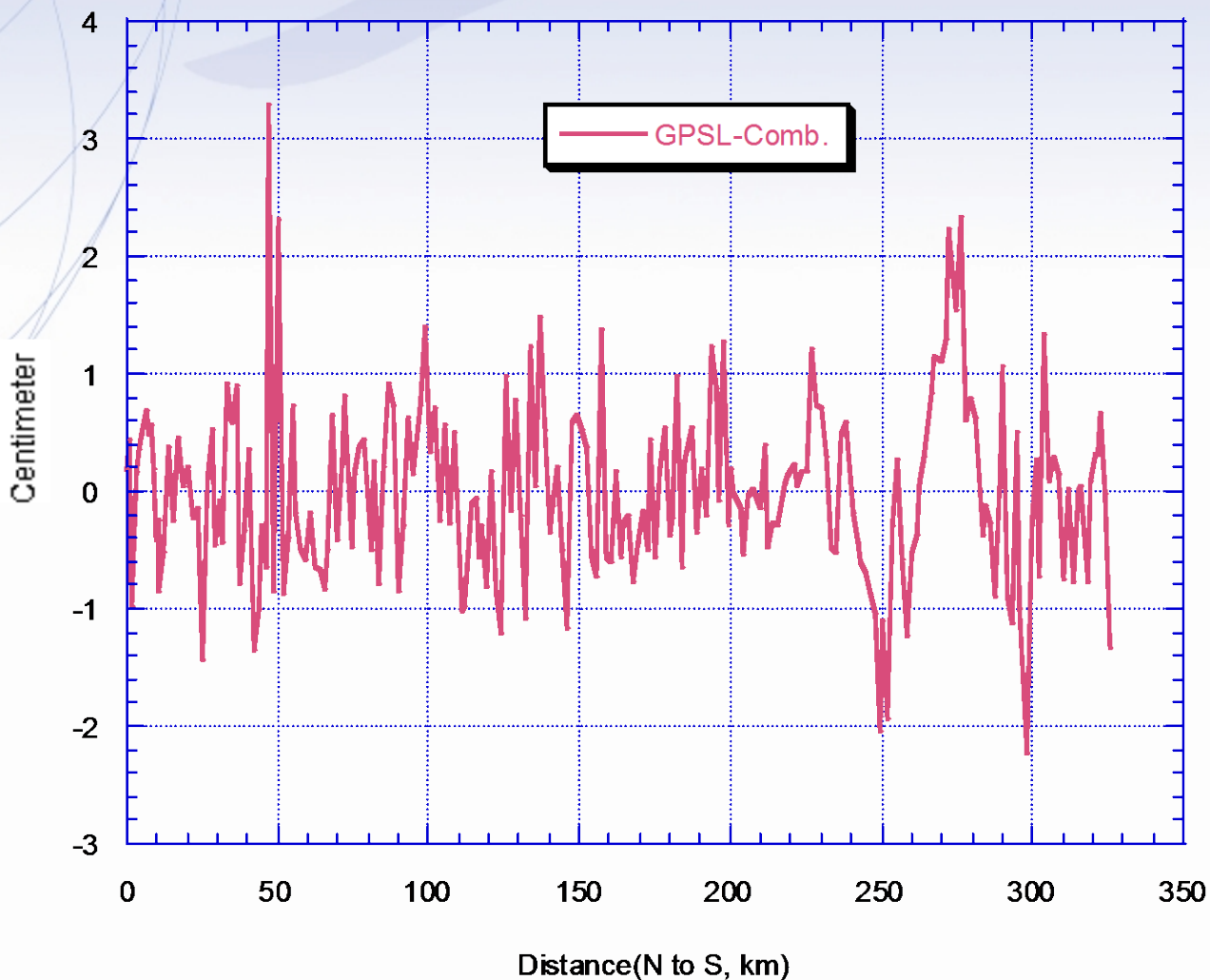
GPSL geoid is accurate at long wavelength, and
DoV geoid is precise at short wavelength:

$$N_{comb} = \sum_{i=0}^N w_i \phi_{GPSL}(f_i) + \sum_{i=0}^N (1 - w_i) \phi_{DoV}(f_i)$$

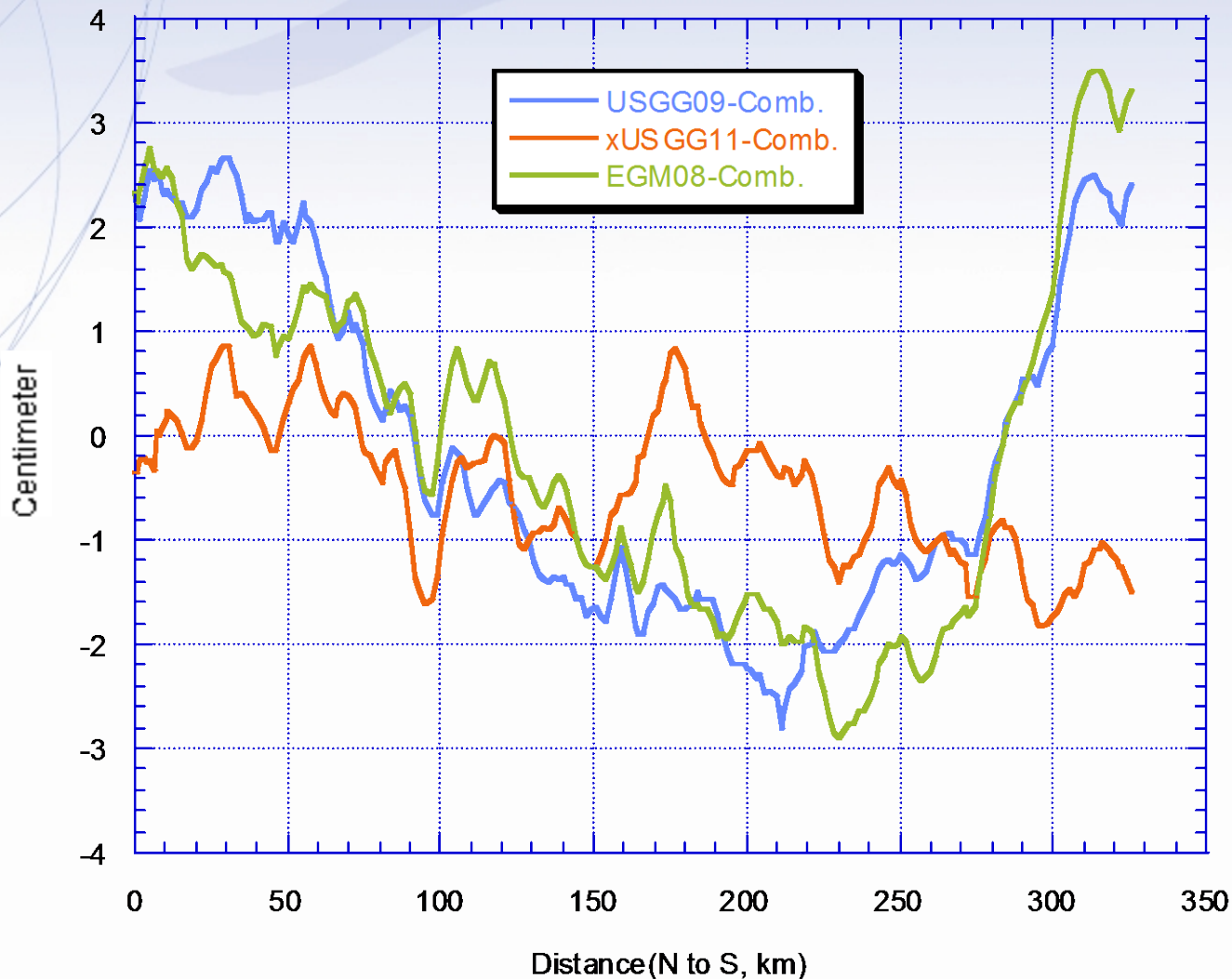
$$w_i = \begin{cases} 1 & i \leq n_0 \\ 0 & i > n_0 \end{cases}$$

where n_0 is the cut-off frequency. The value used in this study corresponds to the wavelength of 96km.

High frequency error removed from GPSL geoid profile



(geoid model – Comb.) along the line



Geoid comparison (model –Comb.)

	GPSL (mm)	USGG09 (mm)	EGM08 (mm)	xUSGG11 (mm)
Mean	-0.0	-0.4	0.1	-0.5
STD	7.6	16.9	17.2	6.7
RMS	7.6	16.9	17.2	8.2
Min.	-22.2	-28.0	-29.1	-18.2
Max.	33.0	26.7	35.1	8.7

Estimation of differential accuracy of the combined geoid profile

$$\begin{aligned}\sigma^2(xUSGG11 - comb) \\ &= \sigma^2(xUSGG11) + \sigma^2(comb) \\ &= 6.7^2 \text{ mm}^2 \\ &\rightarrow \sigma^2(xUSGG11) \leq 6.7^2 \text{ mm}^2 \\ &\quad \sigma^2(comb) \leq 6.7^2 \text{ mm}^2\end{aligned}$$

- Thus, the differential accuracy of the combined geoid profile is probably better than 5mm.
- Then the differential accuracy of xUSGG11 is around 5mm, and can't be worse than 6.7 mm.

Conclusions(1)

- STD values of differences of geoid models and DoV geoid are over 30mm; the GRAV-D airborne gravity data enhanced geoid agrees with GPSL geoid in 9.5mm (STD value).
- The DoV geoid tilt could be attributed to biases of 0.072" (N-S) and 0.019" (E-W) in DoV data.
- The combined geoid (GPSL+DoV) may be better than 5mm of differential accuracy, all high frequency errors in GPSL geoid are removed.

Conclusions(2)

- There is a 0.04 ppm slope between xUSGG11 and GPSL geoid (which one is tilted?)
- GRAV-D airborne gravity data enhanced geoid model xUSGG11 is revealed a differential accuracy of better than 6mm.
- DIADEM camera DoV data could be useful for long traverses if the systematic biases are carefully calibrated.

Future Work

- Investigate the terrain effect on the DoV data interpolation and possible system biases removal
- Combine satellite gravity models (long wavelength) with DoV data (short wavelength) in geoid profile computation